#### Wiktor Zuba

## MIMUW Colloquium

13.03.2025

### Background

- 2011-2021: Studies at MIMUW

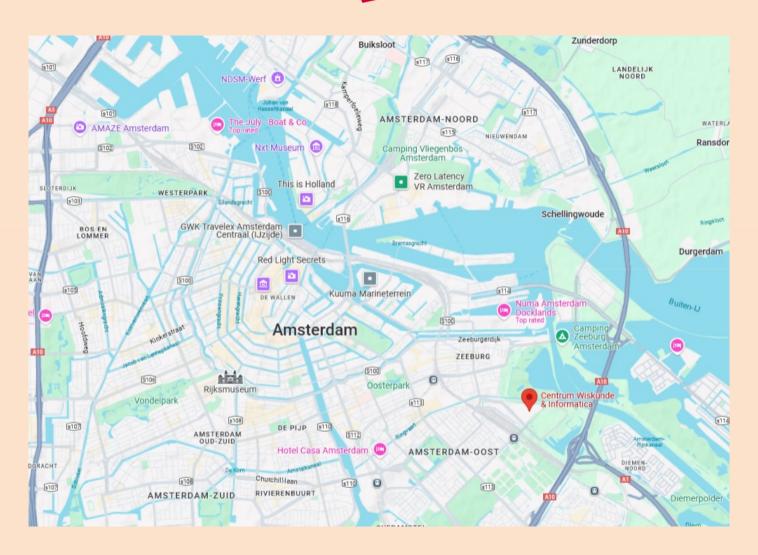
2022-2024: PostDoc at CWI

- 2024-present: Assistant Professor at MIMUW

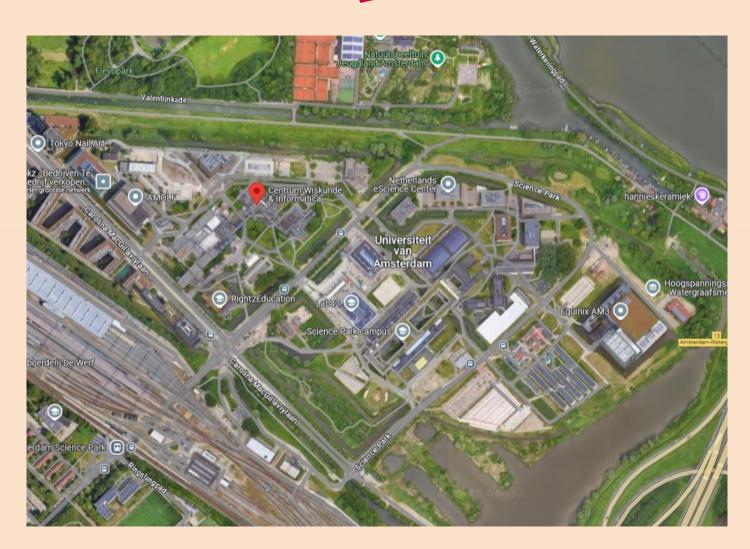










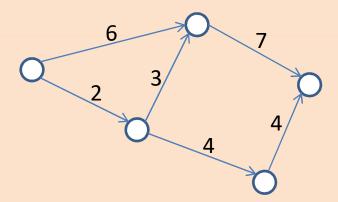




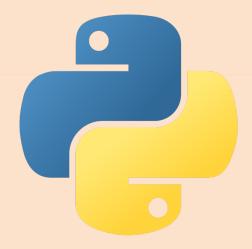




#### Dijkstra Algorithm 1956



#### Python 1980s





#### **Text Algorithms Team**



#### **Text Algorithms Team**



Wojciech Rytter



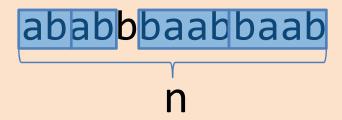
Jakub Radoszewski



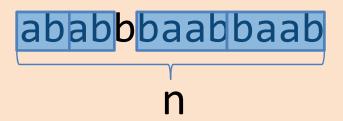
Tomasz Waleń

ababbbaabbaab n

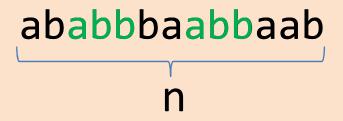
(Check / find all / count all) regular parts

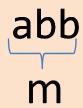


(Check / find all / count all) regular parts



(Check / find all / count all) regular parts (in a substring)

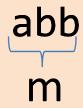




(Check / find all / count all) regular parts (in a substring)

Pattern matching

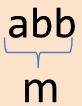
```
abbabbabb abb
ababbbaabbaab
n
```



(Check / find all / count all) regular parts (in a substring)

(Approximate = up to k errors)
Pattern matching

```
abbabbabb abb
ababbbaabbaab
n
```



(Check / find all / count all) regular parts (in a substring)

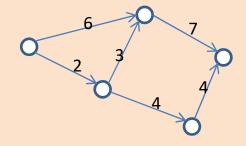
(Approximate = up to k errors)
Pattern matching

String similarities (common substrings, ...)

# Applications of regularities and similarities of strings

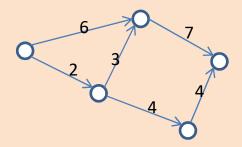
- Bioinformatics tandem repeats are associated to genetic diseases,
   similarities between DNA sequences~ close relationship between organisms
- Compression high regularity = better compression rate
- Data analisys plagiarism detection

#### **Graph algorithms**

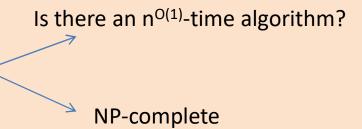


brute force: usually exponential

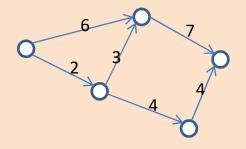
#### **Graph algorithms**



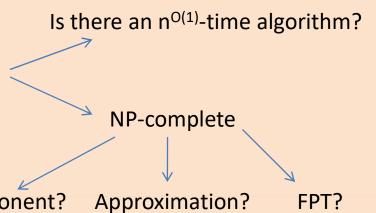
brute force: usually exponential



#### **Graph algorithms**

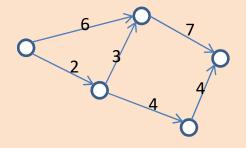


brute force: usually exponential



Smaller exponent? Approximation?

#### **Graph algorithms**



brute force: usually exponential

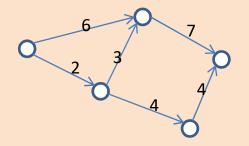
Is there an n<sup>O(1)</sup>-time algorithm? NP-complete Smaller exponent? Approximation? FPT?

Text algorithms

ababbbaabbaab

brute force: usually O(n<sup>3</sup>) or O(n<sup>2</sup>) time.

#### **Graph algorithms**



brute force: usually exponential

Is there an n<sup>O(1)</sup>-time algorithm?

NP-complete

Smaller exponent?

Approximation?

FPT?

Text algorithms

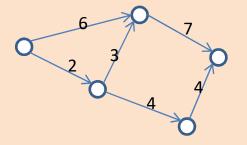
Try to reach O(n) or at least O(n polylog n).

ababbbaabbaab

brute force: usually O(n<sup>3</sup>) or O(n<sup>2</sup>) time.

No  $O(n^{2-\epsilon})$  time algorithm (by e.g. SETH)

#### Graph algorithms



brute force: usually exponential

Is there an n<sup>O(1)</sup>-time algorithm?

NP-complete

Smaller exponent?

Approximation?

FPT?

Text algorithms

Try to reach O(n) or at least O(n polylog n).

ababbbaabbaab

brute force:

usually  $O(n^3)$  or  $O(n^2)$  time. Sometimes even  $O(n/\log n)$ .

No  $O(n^{2-\epsilon})$  time algorithm (by e.g. SETH)

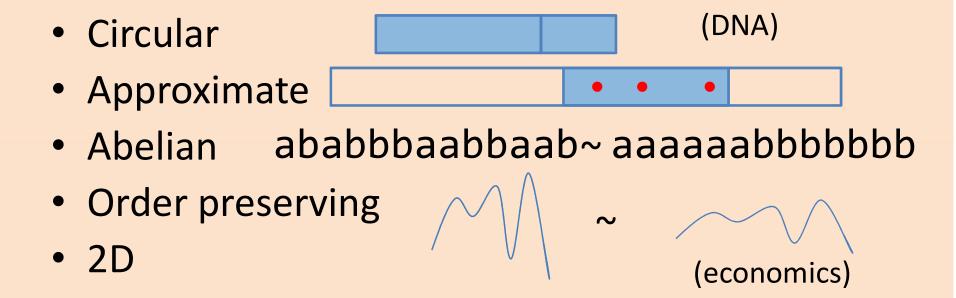
- Circular
- Approximate
- Abelian
- Order preserving
- 2D

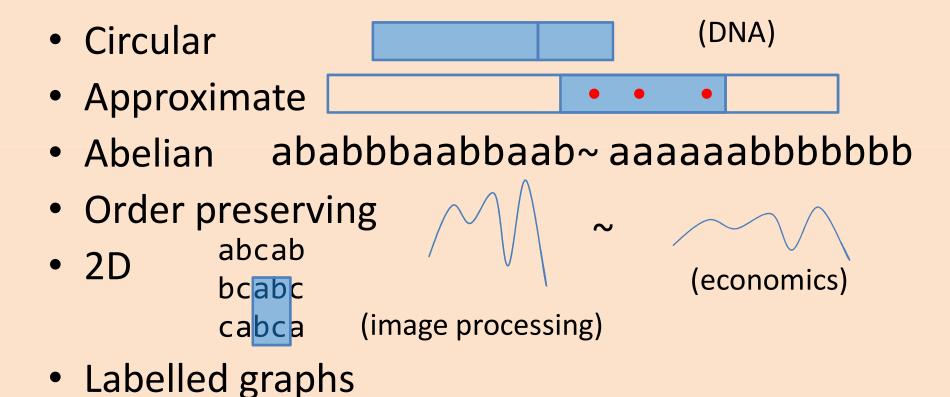


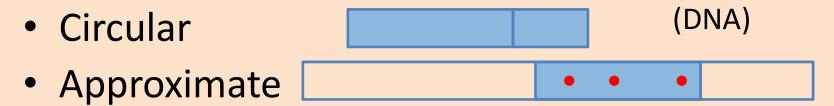
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- CircularApproximate(DNA)
- Abelian
- Order preserving
- 2D

- CircularApproximate(DNA)
- Abelian ababbbaabbaab~ aaaaaabbbbbbbb
- Order preserving
- 2D



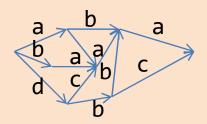




- Abelian ababbbaabbaab~ aaaaabbbbbbbb
- Order preserving
- 2D abcab bcabc cabca

(image processing)

Labelled graphs



(representation of pangenomes)

(economics)

#### RECENT EXAMPLES

(IN MY PUBLICATIONS)

|   |   |     | 3   |     |     |     |
|---|---|-----|-----|-----|-----|-----|
| A | 1 | 1/2 | 3/4 | 4/5 | 1/2 | 1/4 |
| В | 0 | 1/2 | 1/4 | 1/5 | 1/2 | 3/4 |

|   |   |     | 3   |     |     | La contraction of the contractio |
|---|---|-----|-----|-----|-----|--|
| A | 1 | 1/2 | 3/4 | 4/5 | 1/2 | 1/4  |
| В | 0 | 1/2 | 1/4 | 1/5 | 1/2 | 3/4  |

$$P(X[3..5] = ABA) = 3/40$$

|   | 6   | 5   | 4   | 3   | 2   | 1 | X |
|---|-----|-----|-----|-----|-----|---|---|
| P(X[35] = ABA) = 3/40                                       | 1/4 | 1/2 | 4/5 | 3/4 | 1/2 | 1 | A |
| $P(X[35] = ABA) = 3/40$ Occurrence if probablity $\geq 1/2$ | 3/4 | 1/2 | 1/5 | 1/4 | 1/2 | 0 | В |

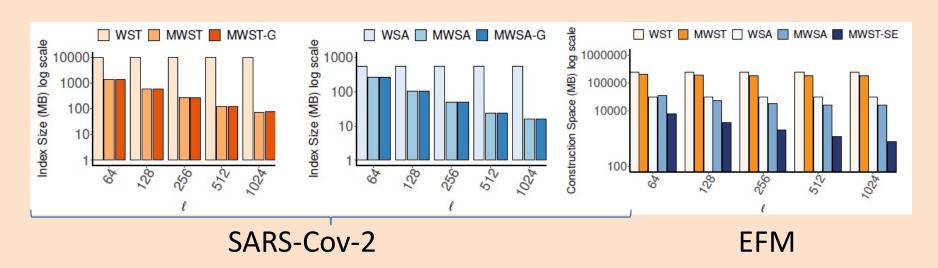
O(nz) size indexes are too large to be useful.

Our result: O(nz/I) size indexes for patterns of length  $\geq I$ .

|  | 6   | 5   | 4   | 3   | 2   | 1 | X |
|--|-----|-----|-----|-----|-----|---|---|
| P(X[35] = ABA) = 3/40  | 1/4 | 1/2 | 4/5 | 3/4 | 1/2 | 1 | A |
| P(X[35] = ABA) = 3/40<br>Occurrence if probablity $\geq 1/z$ | 3/4 | 1/2 | 1/5 | 1/4 | 1/2 | 0 | В |

O(nz) size indexes are too large to be useful.

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## Scalable Order-Preserving Pattern Mining (ICDM 2024)

Pattern mining in time series (IEEE Trans. Cybern. 2023) Their algorithm finds frequent patterns, but it takes  $\Omega(n^3)$  time.

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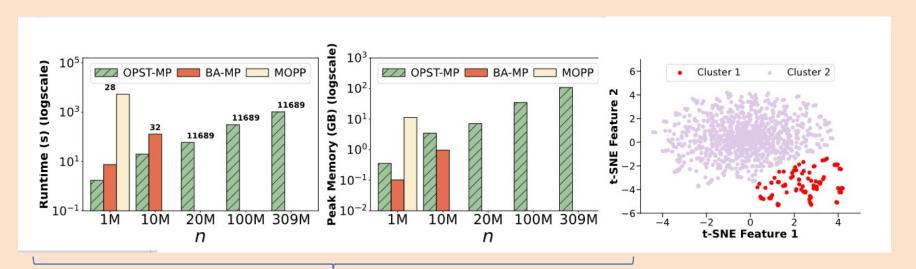
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Thank you for your attention!